

## Adaptive Relay Scheme Based on Channel State in Dual-Hop System

Seung-Jun Yu, Yong-Jun Kim, Hyoung-Kyu Song\*

uT Communication Research Institute, Sejong University, Seoul, Korea

uT Communication Research Institute, Sejong University, Seoul, Korea

uT Communication Research Institute, Sejong University, Seoul, Korea.

\*Corresponding Author's E-mail: [songhk@sejong.ac.kr](mailto:songhk@sejong.ac.kr)

### ABSTRACT

Conventional dual-hop scheme has used the same modulation method for the source and the relays. Given that the distances between the source and the relays are close, in other words, when the quality of the source-relays link is good, the usage of higher order modulation at the source improves total system throughput. However, in opposite case, bit error probability is increased through using higher order modulation. Therefore, we propose a relay scheme that uses hierarchical modulation at the source and adaptive modulation based on the channel state at the relays. Accordingly, the symbol error rate (SER) and throughput performances are improved by the proposed scheme.

**Keywords:** Dual-hop, Relay, Adaptive modulation, Channel state, Hierarchical modulation.

### I. INTRODUCTION

In recent years, using relays in wireless networks has garnered significant interest. It is well known that due to shadowing, multipath fading, distance-dependent path losses and interference, the link quality between the source and destination in a wireless network often degrades severely. In such a scenario, relays can be employed between the source and destination terminals for assisting the transmission of data from the source to destination [1], [2]. In particular, source can cooperate with the relays to relay the replicas of the source signal to the destination thereby providing additional diversity and improved signal quality at the destination. In the literature, various schemes of cooperative communications such as amplify-and-forward (AF), decode-and-forward [2], coded-cooperation [3], and compress-and-forward [4] have been presented. In [5], the outage and ergodic capacities have been analyzed for a three terminal network where one of the relays the messages of another terminals towards the third one. A multiple-input multiple-output (MIMO) relay network [6] is composed of source, relay, and destination terminals, each of which is equipped with multiple antennas. Network information theory has shown that the use of multiple relay terminals in source and destination (S-D) communication makes the capacity of the S-D system logarithmically increase with the number of relay terminals.

A simple description of the dual-hop relaying protocol [7] is following. In the first hop, the source broadcasts to the relays. In the second hop, the relays simply transmit source signals in separated channels or transmit them using a space-time code to the

destination. Consequently, the reliability of the communications is improved whereas the throughput might go down since the transmission is performed by two times. Conventional dual-hop scheme has used the same modulation method for the source and the relays. Given that the distances between the source and the relays are close, in other words, when the quality of the source-relays link is good, the usage of higher order modulation at the source improves total system throughput. However, in opposite case, bit error probability is increased through using higher order modulation. Therefore, we propose a relay scheme that uses hierarchical modulation [7] at the source and adaptive modulation based on the channel state at the relays. Accordingly, the symbol error rate (SER) and throughput performances are improved by the proposed scheme.

### II. SYSTEM MODEL

In this section, we consider a dual-hop relay system with 3 terminals which is made up of a source S, a relay R and a destination D. A source S and a relay R have a single antenna. We assume that communication takes place only over dual-hop links and there is no direct link between S and D. The coefficient of the link between i-th antenna at S and j-th antenna at R is  $g_{i,j}$  and  $h_{i,j}$  is the coefficient of the link between i-th antenna at R and j-th antenna at D, where  $i, j = 1, 2$ . It is assumed that each channel goes through Rayleigh fading and the link coefficients  $g_{i,j}$  and  $h_{i,j}$  are independent and identically distributed (i.i.d). Also, the channel state information (CSI) is known to R and D. We assume a half-duplex channel, for which all terminals cannot transmit and receive symbols at the same time over the same frequency band.

### III. PROPOSED SCHEME

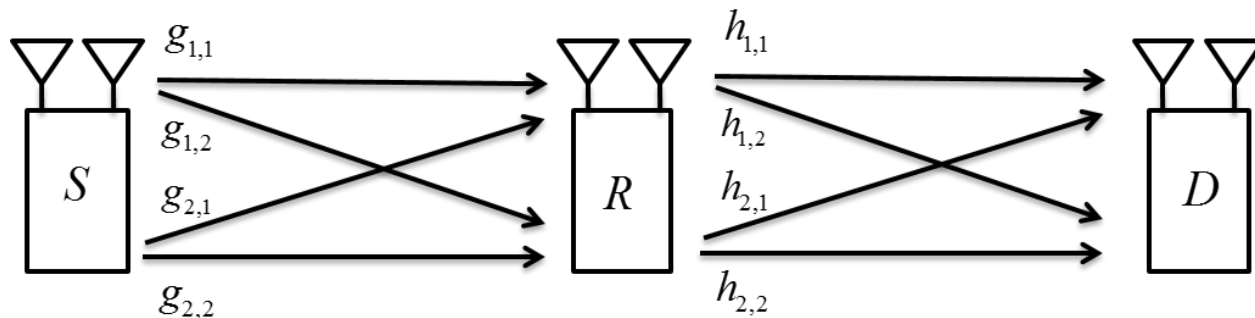


Fig 1: Dual-Hop Relay System

In this section, we propose an adaptive relay scheme based on channel state in dual-hop relay system. The proposed relay scheme provides high throughput in good channel condition and maintain SER performance in bad channel condition. In order to adaptively transmit signals in a relay, the post SNR is calculated. To know the channel state for each subcarrier, post-signal-to-noise ratio (Post SNR) which can be determined by the channel state is used. The post SNR value for  $k$ -th subcarrier ( $\rho_i$ ) is represented as follows,

$$\rho_i = \frac{\|X(k)\|^2}{\sigma_n^2 \|G_i(k)\|^2}, \quad (1)$$

where  $\|X(k)\|^2$  means transmit power of subcarrier,  $\sigma_n^2$  denotes noise power and  $G_i(k)$  is the  $i$ -th row of the Moore-Penrose pseudo-inverse matrix. The noise considered by the minimum mean square error (MMSE) method which can be expressed as,

$$G_{MMSE} = \mathbf{H}^H (\mathbf{H}\mathbf{H}^H + \sigma_n^2 / \sigma_x^2 \mathbf{I}_{N_R})^{-1}, \quad (2)$$

where  $\mathbf{I}$  is identity matrix and the  $\sigma_x^2$  denotes the power for the transmit signal. In Eq. (1), because the transmit signal power is 1, transmit power little impacts on the post SNR. Most impact on the post SNR power value is obtained by a Moore-Penrose pseudo-inverse matrix.

If the  $\|G(k)\|^2$  value is large, the post SNR is to be small and the channel state is determined to poor state. And vice versa, if the  $\|G(k)\|^2$  value is small, the channel state is determined good state.

The proposed scheme uses hierarchical 16-QAM, which can be regarded as the combination of two QPSK modulations. The former 2 bits choose a position of large quadrant and the latter 2 bits determine a position of the small quadrant within the former 2 bits selected position. We name them hierarchical modulation class 1 (HM class 1) and class 2 (HM class 2), respectively. In conventional use of hierarchical 16-QAM, these distinctive classes enable a QPSK or a 16-QAM demodulator according to the channel quality. In contrast to that, we use hierarchical 16-QAM to let a relay always demodulate with a 16-QAM demodulator.

If the  $\|G(k)\|^2$  value is large, a relay discard the latter 2 bits. In voice and video signals, any most significant bits (MSBs) errors cause significantly more degradation in the symbol quality as compared to errors in the least significant bits (LSBs). Let us consider 4 bits data with 2 MSBs and LSBs. In hierarchical 16-QAM, groups of 2 MSBs are mapped to HM class 1 and groups of 2 LSBs are mapped to HM class 2, respectively. Hence, a very small performance drop is caused by omitting the latter 2 bits. For easier understanding of the proposed scheme, a simple relay example which considers a relay with 2 antennas is provided. The proposed scheme may be operated using following steps. A source broadcasts hierarchically 16-QAM modulated symbols  $X_{12}$  and  $X_{34}$  to a relay. The received symbols at a relay in frequency domain are represented as

$$\begin{aligned} Y_{R_1} &= G_{1,1} X_{12} + G_{2,1} X_{34} + N_{R_1}, \\ Y_{R_2} &= G_{1,2} X_{12} + G_{2,2} X_{34} + N_{R_2}, \end{aligned} \quad (3)$$

where the subscript  $R_i$  stands at the  $i$ -th antenna in a relay,  $G_{i,j}$  represents the frequency responses of link between  $i$ -th antenna at  $S$  and  $j$ -th antenna at  $R$  and  $N$  is a complex Gaussian random variable with zero mean and variance  $\sigma^2$ .

A relay demodulates symbols with a 16-QAM demodulator and uses an adaptive modulation method according to the channel state. If the measured post SNR is large at a relay, a relay modulates 4 bits with a 16-QAM modulator. If the measured post SNR is small at a relay, a relay discard latter 2 bits. And then, a relay modulates former 2 bits with a QPSK modulator. Modulated symbols are implemented by using IFFT of size  $N_F$  in a relay. The code design of the relay which has a large post SNR is

$$M = \begin{pmatrix} X_{12} \\ X_{34} \end{pmatrix}, \quad (4)$$

The code design of the relay which has a small post SNR is

$$M = \begin{pmatrix} X_1 \\ X_3 \end{pmatrix}, \quad (5)$$

At second time slot, the destination receives adaptive modulated symbols from a relay. In case of a large post SNR, the received symbols in the frequency domain can be expressed as

$$Y_{D_1} = H_{1,1} X_{12} + H_{2,1} X_{34} + N_{R_1}, \quad (6)$$

$$Y_{D_2} = H_{1,2} X_{12} + H_{2,2} X_{34} + N_{R_2},$$

where  $D_n$  is an index of the  $n$ -th destination antenna,  $H_{i,j}$  is the channel frequency response of link between  $i$ -th antenna at R and  $j$ -th antenna at D, and  $N$  is a complex Gaussian random variable with zero mean and variance  $\sigma^2$ .

In case of a small post SNR, the received symbols in the frequency domain can be expressed as

$$Y_{D_1} = H_{1,1} X_1 + H_{2,1} X_3 + N_{R_1}, \quad (6)$$

$$Y_{D_2} = H_{1,2} X_1 + H_{2,2} X_3 + N_{R_2},$$

Finally, we can reconstruct the original signal with simple V-BLAST detection algorithm in a destination. The linear scheme with MMSE is used. The MMSE Moore-Penrose pseudo-inverse matrix is as

$$\mathbf{G}_{MMSE} = \mathbf{H}^H (\mathbf{H}\mathbf{H}^H + \sigma_n^2 / \sigma_x^2 \mathbf{I}_{N_R})^{-1}, \quad (7)$$

where  $(\cdot)^H$  is the conjugate transpose operation. Finally, the estimated symbols are as

$$\begin{bmatrix} \hat{X}_{12} \\ \hat{X}_{34} \end{bmatrix} = \mathbf{G}_{MMSE} \begin{bmatrix} Y_{D_1} \\ Y_{D_2} \end{bmatrix}. \quad (8)$$

#### IV. SIMULATION RESULTS

In the relay model, we consider perfect synchronization and complete equalization. Moreover, the total power of the transmitting terminals is the same as the transmit power of a single hop transmission for pair comparison and all terminals have the same noise characteristics. Simulations are accomplished with following parameters. The fast Fourier transform (FFT) size is 128 and the cyclic prefix (CP) length is 32. For simulations, a source, a relay and a destination terminal are used over 8-path Rayleigh fading channel. Fig. 2 shows the SER performance of the proposed scheme. In the simulation, depending on the channel state, a relay adaptively transmits modulated symbols. Consequently, the proposed scheme shows higher SER performance than that of the conventional scheme.

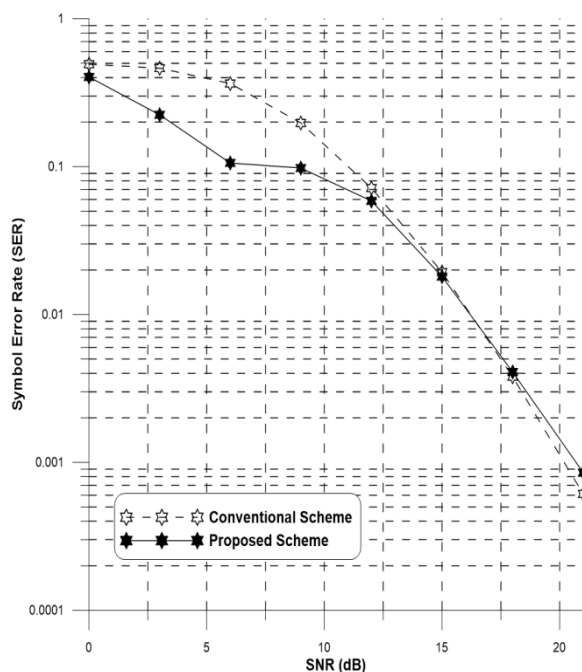


Fig 2: The SER performance of the proposed scheme

#### V. CONCLUSION

In this paper, we propose an adaptive relay scheme based on channel state in dual-hop system. The simulation result has shown that the SER performance of the proposed scheme is improved by using an adaptive modulation. In particular, the proposed scheme guarantees reliable transmission for low SNR.

#### VI. ACKNOWLEDGMENTS

This work was supported by the IT R&D program of MOTIE/KEIT [10054819, Development of modular wearable platform technology for the disaster and industrial site] and by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Science, ICT and future Planning (No. 2013R1A2A2A01067708).

#### REFERENCES

- [1] Laneman, J. N., Wornell, G. W., and Tse, D. N. C. 2001. An efficient protocol for realizing cooperative diversity in wireless networks. In Proc. Int. Symp. Inf. Theory
- [2] Laneman, J. N. and Wornell, G. W. 2000. Exploiting distributed spatial diversity in wireless networks. In Proc. Allerton conf. Comm.
- [3] Janani, M., Hedayat, A., Hunter, T. E., and Nosratinia, A. 2004. Coded cooperation in wireless communications: Space-time transmission and iterative decoding. IEEE

- Trans. Signal Process. 52 (Feb. 2004), 362 - 371.
- [4] Kramer, G., Gastpar, M., and Gupta, P. 2005. Cooperative strategies and capacity theorem for relay networks. *IEEE Trans. Inf. Theory*. 51 (Sep. 2005), 3037 - 3063.
- [5] Nabar, R. U., Bölcskei, H., and Kneubühler, F. W. 2004. Fading relay channels: Performance limits and space-time signal design. *IEEE J. Sel. Areas Commun.* 22 (Aug. 2004), 1099 - 1109.
- [6] Abe, T., Hui, S., Asai, T., Yoshino, H. 2005. A Relaying Scheme for MIMO Wireless Networks with Multiple Source and Destination Pairs. In *Proc. Asia-Pacific Conference on Communications*
- [7] Shin, J.-C., Song, J.-H., Kim, J.-H., and Song, H.-K. 2010. Dual-Hop Transmission Scheme Based on Hierarchical Modulation in Wireless Networks. 2010. *IEICE Trans. Commun.* E93-B (June 2010), 1645 – 1648.